Problem Set 2

Due 2/26/96 in class or by 5 p.m. to Michael Kreutz, E52-251

Theory

- 1. Nicholson, Problems 3.2, 3.4, 4.4, 4.5, and 5.8.
- 2. Let $U(X,Y) = X^{1/4}Y^{3/4}$. Suppose that prices are P_x and P_y , and income is I. Calculate the utility-maximizing choices of X and Y, that is, the Marshallian demand functions $d_x(P_x,P_y,I)$ and $d_y(P_x,P_y,I)$.
 - (a) Calculate "indirect utility," or the utility at the optimal choices, $V(P_x, P_y, I)$.
 - (b) For a given utility level U_0 , solve the dual expenditure-minimization problem, and compute the optimal choices of X and Y (the "compensated demand functions," $h_x(P_x,P_y,U_0)$ and $h_y(P_x,P_y,U_0)$).
 - (c) Calculate the minimum expenditure function $E(P_x, P_y, U_0)$. Show that the expenditure and indirect utility functions you have calculated are inverses of one another.
 - (d) Consider two famous applications of the envelope theorem in consumer theory, Shephard's Lemma and Roy's Identity ((E5.1) and (E5.2) in Nicholson). State a verbal interpretation of each of these results.
 - (e) Verify directly that Shephard's Lemma and Roy's Identity hold in this problem.

Application ("Irish Potato" article)

- 1. Draw a diagram illustrating Giffen's paradox. Your diagram should illustrate a consumer's 2-good utility maximization problem for two different budget constraints, where P_x is higher under the second constraint.
- 2. Consider Figure 1 of Dwyer and Lindsay. Explain why the top diagram is consistent with the your diagram from question (1). Why is the lower diagram a better description of the Irish potato famine?
- 3. Dwyer and Lindsay make two claims about Giffen goods: "For a good to be Giffen, some normal good must be displaced by the inferior good as the price rise lowers real income." "Inferiority is necessary for a good to be Giffen." Formally prove these two statements, and then briefly state a reason why each is unlikely to hold for the case of the Irish potato famine.
- 4. We are interested in measuring the effects of a price change on the amount demanded of potatoes. Graph the budget constraint facing a person with income *I* and the ability to purchase potatoes and bread if the price of bread is \$1.00 and the cost of potatoes is *P*. Draw a standard set of indifference curves and illustrate the optimal bundle.