

Ideological Competition

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Abstract: *We propose a model of political competition not over policy programs, but over ideologies: models of the world that organize voters' experiences and guide the inferences they draw from observed outcomes. Policy-motivated political parties develop ideologies, and voters choose the ideology that best explains their observations. Preferences over policies are then induced by the adopted ideology. Parties thus care about winning the ideological battle as it confers an advantage in the electoral arena. We show that in equilibrium political parties always propose different models of the world. This divergence extends to all features of the environment, not just policy dimensions. A lower degree of policy extremism in the past increases the divergence on the policy dimension, thus leading to higher ideological polarization.*

How do citizens form policy preferences? The question has been a central one in political science since the discipline's behavioral turn in the mid-twentieth century. Indeed, democratic citizenship confronts the mass public with a difficult problem: How to evaluate policy alternatives with which they may lack familiarity, experience, or basic understanding.

A half-century of research effort has produced a rich and varied set of answers. Scholars have variously argued that citizens have policy preferences that are temporally unstable, if they can be said to exist at all (Converse 1964), formed on the spot when prompted (Zaller 1992), formed by following elite cues (Brady and Sniderman 1985; Lenz 2013), or considered in reaction when politics intrudes into life unbidden (Klar and Krupnikov 2016).

The classical formal treatments of political competition under complete information (Downs 1957), on the other hand, sidestep the question of the origin of policy preferences, instead taking them as exogenous and fixed model primitives. This approach has proved fruitful for deriving predictions about the relationship of outcomes to the distribution of preferences in the population. But it considerably narrows the scope of political inquiry, and renders opaque much of the day-to-day work that polit-

ical practitioners invest in campaigning, organizing, and honing rhetorical arguments.

In this article, we aim at bridging this gap by offering a formal model of policy preference formation embedded in a political competition framework. Our model is a hierarchical one, in which citizens first choose ideologies—systems of belief about the underlying process that generates social outcomes—and then apply those ideologies to decide which policy inputs they prefer. Ideology thus provides a narrative that allows citizens to “navigate and orient themselves in the sea of politics” (Sartori 1969). By providing a theory of how the world works, ideologies enable citizens to form expectations about the consequences of the various policy choices, which in turn inform their policy preferences. By their nature, such ideologically *induced* preferences are contingent and flexible, and subject to the kinds of temporal shifts and responses to elite signals that the behaviorists have documented.

This conception of ideology as distinct from and prior to policy preferences delivers a very different view of the nature of political competition among party leaders, which contrasts sharply with canonical formal treatments. Where the traditional approach views parties as strategically choosing platforms to assemble a winning electoral coalition, our model highlights the role of

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¹This is akin to what Gramsci (1929) refers to as cultural hegemony: The elite construct ideological worldviews to impose their belief systems to the people, and thus achieve and maintain control even without the use of coercive means.

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parties in developing political narratives, with the aim of manipulating and directing the masses.¹ Importantly, the parties' ability to persuade voters does not come from an information asymmetry, but rather from their role as ideological entrepreneurs: Parties have monopoly power over the development of ideologies.

Our model thus reverses the logic of standard formal models of elections. In our world, the parties' strategic problem is not solely to choose a policy platform that appeals to exogenous citizen preferences. Rather, political parties try to generate a favorable electoral environment by inducing citizens to adopt an ideology that translates into preferences aligned with the party's own policy program. The parties compete over ideology, not because they care about ideology *per se* but because ideology shapes the subsequent policy competition. A party that can win the ideological battle, so to speak, attains a favorable position in the policy competition. Ideology will thus be an equilibrium outcome of our model, rather than one of its primitives.

Operationalizing Political Ideology. Political ideology is a concept that is at once familiar yet difficult to pin down. As Sartori (1969) drily notes, "the growing popularity of the term has been matched, if anything, by its growing obscurity." Gerring (1997, p. 980) contends that the element common to all definitions of ideology is coherence, that a citizen's values, her understanding of the world, and the policy preferences she holds are "bound together." Narrower definitions of ideology take values as fixed and focus on how ideology translates those values to policy preferences (Freedman 2001), whereas broader definitions encompass the construction of values as well (Knight 2006).

In this article, we operationalize ideology in the narrower sense. We take a citizen's objective—and, thus, her values—as given and think about ideology as translating values into policy preferences.² At this level, an ideology is a system of beliefs about the underlying process that generates social outcomes and that citizens use to map their values into concrete policy preferences.

Politicians in practice devote considerable effort to shaping ideological beliefs. These efforts manifest as arguments for how the world works and why it looks the way it does, and are often devoid of specific policy content. Illustrative examples come from the political rhetoric of Margaret Thatcher on one side of the political spectrum, and Bernie Sanders on the other. In 1987,

then-Prime Minister and leader of the U.K. Conservative Party Margaret Thatcher famously stated her disbelief in the existence of society: "[Too many people] are casting their problems on society and who is society? There is no such thing! There are individual men and women and there are families." The statement contains no reference to any particular policy or element of the Tory platform. It instead invites the audience to adopt a particular model of the causal forces that underlie the variation in outcomes they observe in the world: If some are rich, and others poor, it must be because of immutable differences in individual abilities or talents and not societal factors amenable to democratic control.

Almost 30 years later, Sanders' rhetoric offered a moral vision almost a mirror image of the one offered by Thatcher: "I believe. . . we are in this together. These are not just words. The truth is on some level when you hurt, when your children hurt, I hurt. And when my kids hurt, you hurt." The statement makes what amounts to an empirical claim: that our well-being (or the absence of "hurt," in Sanders' formulation) is not driven solely by our own income or consumption but by the well-being of everyone we interact with. The Vermont Senator thus offers a theory of the world but, again, no specific policy prescription.

Sophisticated observers often lament that policy-free statements like these reflect a superficial or dumbed-down approach to politics. By taking seriously the role of ideology, we argue that much of this rhetoric is, in fact, highly policy relevant. The policy stakes of such rhetoric can be extremely stark: consider Bonilla-Silva's (1997) account of racial ideology, which argues that it is only after society accepts the placement of people into racial categories that racist policy preferences can emerge.³ By shaping how citizens view the world, politicians can indirectly shape their policy preferences, and do so more persuasively than by appealing to policy directly.

Modeling Ideological Competition. Building on this operationalization of ideology, our contribution is to understand what ideologies and policies emerge from political competition. Our model has three essential elements. First, we conceive of political parties as ideological entrepreneurs, creating and competing on ideology in addition to the traditional competition over policy. Specifically, each party develops and offers to

²We therefore set aside, at least for the moment, questions of where those values originate from and how elites can shape values. We take up these ideas briefly in the concluding discussion.

³Bonilla-Silva (1997) argues that "The placement of groups of people in racial categories stemmed initially from the interests of powerful actors in the social system" (p. 473), and that "Categories such as 'Indians' and 'Negroes' were invented in the sixteenth and seventeenth centuries to justify the conquest and exploitation of various peoples" (p. 471).

the public a theory of the world. The goal is to have the public accept a party's ideology, to adopt its system of beliefs and view of the world and, thus, to shape the policy preferences that the public forms. Winning the ideological competition puts a party in a favorable position for the electoral competition stage that follows.

The second essential element of our model is that citizens are initially "ideologically innocent" (Kinder and Kalmoe 2017), in the sense that they have no ideology of their own, and cannot or will not do the work of developing a theory of the world. In other words, parties have monopoly power over the construction of new ideologies. Citizens can evaluate an ideology if one is offered to them, but they cannot construct their own.

Although this technological advantage gives parties the chance to influence citizens' (induced) preferences, this power is not unconstrained. The third key element of our model is a common-knowledge history of outcomes observed in the past, against which citizens will test the plausibility of parties' models. Our citizens adopt the model of the world that best resonates with their own lived experience and the past experience they absorb from the media and their schooling. This shared historical memory constrains and disciplines parties' ability to persuade.

Overview of Results. In this setting, we show that ideological competition matters for political outcomes. In equilibrium, the two competing parties offer distinct ideologies, with each offering a view of the world in which its preferred policies are more attractive to voters. In particular, we show that the true model of the world never emerges in equilibrium. Although the parties are constrained by history, and voters evaluate ideologies with open eyes, the finiteness of history provides freedom to the parties to offer an explanation of the world that is more favorable to them. The limitations of history provide the space for the emergence of radically different ideologies, such as Margaret Thatcher's individualism or Bernie Sanders' collectivistic view.

Thus, political ideologies are polarized in equilibrium just as are policy preferences. We show that the difference between the ideologies offered in equilibrium is a function of the history of policy choices: Ideological polarization emerges from the narrowness of policy experience. The intuition is that historical data generated under moderate policies are less informative, and this allows parties to persuade voters with more extreme ideologies farther from the best fitting model in the data. Our model shows, therefore, that it is exactly following periods of moderation in policy that we should

expect political parties to espouse radically different ideologies.

Further, we show that ideologies are not limited to policy variables. Acting as ideological entrepreneurs, parties will include nonpolicy variables, over which they have no control or preferences, into their ideologies. They do so in order to shift blame for policy failures onto unrelated factors. This force is strong enough that in equilibrium, ideologies are always total: *All* available dimensions, including those that are not inherently political, are drawn in to parties' models and become sites of ideological conflict. Hence, even if the policy choice can be described by a single dimension, the political domain is inherently multidimensional. This result resonates with work on affective polarization, such as Mason's (2018) study of the politicization of identity characteristics with no inherent connection to policy disagreements.

Our results illuminate the logic behind such social polarization, and allow us to make predictions about which identity attributes are likely to become woven into ideological disagreements, and when. We show that nonpolicy variables are incorporated in the parties' political narratives when their historical correlation with the policy dimension is sufficiently high. This allows parties to use the nonpolicy variables to improve the overall fit of their model, and thus offer even more favorable—and extreme—ideologies on the policy dimension.

In our model, parties have no control over nonpolicy dimensions. Thus, if a strong enough historical correlation with the policy variable emerges, it is purely by chance. The results thus highlight the importance of path dependence and random events in the genesis of political ideologies. Political parties, acting as ideological entrepreneurs, will exploit emergent correlations to construct complex models of the world that support their favored policy position. This process generates a relationship between complexity and ideological polarization: The higher the number of politically salient dimensions (i.e., dimensions included in the proposed model of the world by at least one of the parties), the higher is polarization on the policy dimension in equilibrium.

Perspectives on Our Approach. In the formal theory literature, ideology and policy preferences are typically collapsed into a single characteristic. This is not a requirement of formal theory per se, but of the often embedded assumption that voters are fully rational information processors and decision makers. Under this assumption, all information from history, from voters' experience, from the various political actors, and so on can be processed and collapsed into a final policy

preference. We argue that ideology plays a distinct role in this process.

Our approach accords with the foundational work of Simon (1955) and the behaviorist tradition. That literature has emphasized the difficulty voters have in understanding politics and forming preferences over political objects. The mapping between policies and outcomes is fundamentally uncertain (Callander 2011), and even voters who are well-informed about policies that have been tried in the past face a challenge of using this information to develop preferences about what policies to implement in the future.

Conceptualizing ideologies as worldviews, our work connects with a recent literature in behavioral economics that explores the role of models in decision making.⁴ In this literature, economic agents, as voters do in our model, use data to select a model through which to view the world. The behavioral limitations of agents in these models differ from those that affect voters in our model and we also differ in our focus on the competition among elites in shaping how citizens view the world; see, for example, Mullainathan, Schwartzstein, and Shleifer (2008), Ortoleva (2012), and Schwartzstein and Sunderam (2021).

We are also distinct from the strand of that literature that connects to political economy. Eliaz and Spiegler (2020) focus on causal models that form narratives about politics. Benabou and Tirole (2006) explore citizens' view of how just the world is, developing a model of motivated reasoning in which voters distort or ignore information that does not fit with their preferred view of the world. Closest to our work is Levy, Razin, and Young (2022), but there the distinction is between people with either complex or simple views of the world and not between elites and the masses.

Indeed, we follow the strand of the behavioral literature that emphasizes the role leaders and elites play in helping voters make sense of the political world, providing a specific channel—the formation of ideologies—through which this occurs. Our formulation reflects the power of elites while also acknowledging its limits. Ample evidence exists that citizens process information and events themselves and that although they are influenced by elites, perhaps heavily, they do not do so blindly (Bullock 2011). Voters are led, to be sure, but only willingly and with open eyes.

⁴The notion of ideology as shaping voters' interpretation of the observed reality distinguishes our work from Hafer and Landa (2007). Hafer and Landa (2007) also see ideology and beliefs as closely connected, but conceptualize ideology as a person's innate propensity to be persuaded by a left-wing or a right-wing argument.

The Baseline One-Dimensional Model

The model describes a one-period, two-stage game. The players are two policy-motivated parties (R and L), and a representative voter. At the beginning of the game, the players observe a public record of T policies (z) and associated outcomes (y), indexed by $t \in \{-T, \dots, -1\}$. As the notation suggests, we think of these as a history of past policy–outcome pairs, but this interpretation is not essential; the record might instead represent cross-sectional information from policies and outcomes in different countries or states. In addition, the voter privately observes the outcome of the (exogenous) policy that is in place in the first stage (z_0).

Voters in the model have no intrinsic preferences over z . Instead, they care exclusively about outcomes. Preferences over policies will then be fully determined by voters' beliefs about the relationship of policy to outcome.

We model the data-generating process in a simple way: Outcomes y_t are a linear function of the chosen policy z_t and a noise term ε_t .⁵

$$y_t = \beta_0 z_t + \varepsilon_t, \quad (1)$$

where ε_t is i.i.d. from a normal distribution with mean 0 and variance σ^2 . β_0 here is a scalar representing the (expected) change in outcomes resulting from a one-unit change in the policy variable z . Although the baseline model is one-dimensional, that is, assumes that outcomes are only a function of a single (policy) variable, an extension presented below generalizes Equation (1) to include a (possibly multidimensional) set of non-policy covariates.

The ideological contest. The first stage of the model is the ideological contest. The two parties move simultaneously, each proposing an ideology, that is, a model of the world. In this one-dimensional setup, a model of the world is simply a scalar indicating the slope of the policy-mapping function. We denote the ideology proposed by party i as β_i . The voter faces some uncertainty about the data-generating process underlying outcomes. Formally, we assume that the voter does not know the slope of the mapping function, that is, the coefficient β_0 .

We make two restrictions on the way that voters can use information from the past history in evaluating the parties' proposals. First, we do not specify the voter's

⁵The policy dimension here is abstract and need not map one-to-one onto a real-world policy instrument. The important feature for our purposes is that it captures a dimension on which the parties disagree and over which they will have control once in power.

complete beliefs over the true model of the world (i.e., the true β_0). Rather than the usual assumption of Bayesian voters, ours are frequentists. They will evaluate point models in terms of their likelihood, but will not hold a complete probability distribution over the full space of possible models.

Second, we do not allow the voter to freely choose her own ideology from \mathcal{R} . Instead, she must adopt one of the two ideologies proposed by the parties: The choice is a discrete rather than continuous one. This limitation is motivated by the classic activist's observation that political consciousness rarely forms spontaneously, but requires leadership to be expressed,⁶ and the more modern social–scientific observation that most citizens invest little effort in paying attention to politics or in developing their own political ideas. Ideologies offered by the parties are free, from the voter's perspective, whereas developing an alternative requires effort. We assume the cost of such effort is high enough that the voter will not opt to pay it.

This combination implies that the voter will adopt the ideology, among those offered by the parties, which has the highest likelihood given the data she observes.⁷ Given the assumption that the noise term is normally distributed, this implies that the voter adopts the model of the world proposed by R if and only if

$$-\sum_{t=-T}^0 (z_t \beta_R - y_t)^2 > -\sum_{t=-T}^0 (z_t \beta_L - y_t)^2.$$

Notice that the history of outcomes considered by the voter includes the past record of T outcomes and $T + 1$ policy choices that are publicly observed, plus the outcome y_0 , which is privately observed by the voter.

The ideological contest stage is described visually in Figure 1. In one dimension, the history takes the form of a scatterplot, and ideologies take the form of scalars (representing the slope of the line connecting policy and outcome).

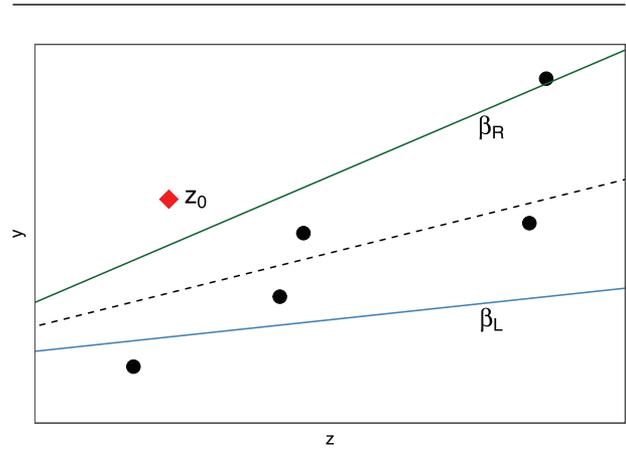
The election. The second stage of the model is the election. The voter casts her vote for one of the two parties. The winner then implements a policy $z_1 \in \mathbb{R}$. We assume that parties have no credible commitment ability, and thus once in power will implement their bliss point.⁸

⁶E.g., Marx in *The Eighteenth Brumaire of Louis Bonaparte* analogized the French agrarian peasantry to a “sack of potatoes,” atomized and unaware of their shared class position and material interests.

⁷Because the voter's utility is linear, this would also be the optimal behavior for a Bayesian voter with a diffuse prior over β_0 .

⁸The assumption of no commitment simplifies the analysis and allows us to focus attention on the ideological stage, but is not crucial. We relax this assumption in the Supporting Information (SI,

FIGURE 1 A Visual Depiction of the Ideological Contest in One Dimension



Notes: Voter and both parties observe the policy–outcome pairs represented by the black dots; the voter privately observes an additional outcome realization at z_0 , the policy in place at time 0 (the red diamond). Parties L and R offer ideologies, in one dimension representable by scalars β_R and β_L (the slope of the line connecting policy and outcome) that center around the expected OLS fit (the dashed line).

Payoffs. The parties are purely policy motivated, with quadratic loss utility: $U_i = -(z_1 - z^i)^2$. z^i denotes party i 's preferred policy. Assume $z^R > z^L$.

The voter cares only about outcomes. In particular, we interpret outcomes y_t as a measure of the voter's welfare. For simplicity, her utility is simply equal to y_t . Given her ideology β_w , and the implemented policy z_1 the voter's expected policy utility is then $\beta_w z_1$.⁹

In addition, the voter's evaluation of the right-wing party is subject to an idiosyncratic shock $\xi \sim U[-\frac{1}{2\psi}, \frac{1}{2\psi}]$.

To sum up, the game proceeds as follows:

1. The players observe a public record of $T < \infty$ policy–outcome pairs, as well as the (exogenous) policy z_0 .
2. The two parties propose their models of the world $\beta_R, \beta_L \in Z \subset \mathbb{R}$.
3. The voter privately observes outcome realization y_0 .

p. 15), and discuss the robustness of the results in this richer environment in a separate section below.

⁹Our results do not depend on the assumption that the voter's utility is defined over outcomes, or that it is linear in z_t . For example, we could assume the voter has single-peaked utility over the policy space, with her ideal policy a function of her ideology β_w . As we show in Appendix E.1 (SI p. 14), this alternative version of the model is essentially isomorphic to the one presented here, and all of our results survive.

4. The voter adopts the model with best fit to observed history $\beta_w \in \{\beta_R, \beta_L\}$.
5. The idiosyncratic preference shock ξ realizes.
6. The voter elects party R or L .
7. The winner implements policy $z_1 \in \mathbb{R}$.

For simplicity, we will assume that the parties know the true value of the coefficient β_0 , although this is not essential to our story or our results. Because we do not allow the voter to draw inferences about β_0 from the parties' proposals, our solution concept is subgame perfect Nash equilibrium.

Analysis

We now describe the formal analysis of the game and the derivation of comparative statics. All proofs are in the SI (pp. 1–14).

As usual, we proceed by backwards induction, beginning with the election winner's policy choice. Our parties do not have credible commitment ability. Straightforwardly, the election winner will therefore always implement its own preferred policy.

The Election

Moving one step backward, consider the voter's problem at the electoral stage. Having adopted ideology β_w , and anticipating the equilibrium policy choice of the two parties, the voter can compute the expected outcome under R and L . Thus, her expected policy utility from electing the right-wing party R is $\beta_w z^R$. Similarly, her expected utility from electing L is simply $\beta_w z^L$. Further, recall that the voter's evaluation of the right-wing party is subject to the idiosyncratic shock ξ . Thus, in equilibrium the voter chooses to elect the right-wing party if and only if

$$\beta_w z^R + \xi > \beta_w z^L. \quad (2)$$

From the parties' perspective, the election is probabilistic: Even after conditioning on the voter's ideology, the election outcome depends on the realization of the shock ξ . Nonetheless, winning the ideological battle gives an electoral advantage.

Proposition 1. *The probability that the right-wing party wins the election is linearly increasing in β_w . Specifically, the probability that R wins the election is given by:*

$$\mathbb{P}_R = \frac{1}{2} + \psi \beta_w (z^R - z^L). \quad (3)$$

Recall that $z^R > z^L$. A direct implication of Proposition 1 is that the right-wing (left-wing) party's expected utility is linearly increasing (decreasing) in β_w . The larger the (absolute) value of β_w , the larger the difference in the voter's expected utility from the two parties. The right-wing party thus wants the voter to adopt an extreme right-wing ideology, as this insures against unfavorable realizations of the shock ξ . A symmetric reasoning holds for the left-wing party L . Thus, both parties have a preference for inducing extreme (and directionally opposed) ideologies.

The Ideological Contest

Let us now consider the strategic problem the parties face in the ideological contest. Each party wants the voter to adopt an extreme and favorable ideology. However, parties compete with each other over ideological influence, and must consider how proposing an extreme ideology influences their chances of persuading the voter, which depend on the expected fit of the proposed model to the history of outcomes. Crucially, although the parties observe the public record of past policies and outcomes, the outcome of the policy z_0 in place at the beginning of the game is privately observed by the voter. For any pair of proposed models, the parties are therefore unsure of which one will best explain the outcomes observed by the voter. They must trade off the probability of convincing the voter against the amount of extremism induced in the voter's beliefs.

Proposition 2 is a direct consequence of this uncertainty and the resulting tradeoff.

Proposition 2. *An equilibrium exists for any $T \geq 1$. The (unique) equilibrium can be characterized by the following:*

1. *The two parties never propose the same model of the world: Ideological polarization always emerges in equilibrium. $\beta_R^* > \beta_L^*$.*
2. *The parties always win the ideological contest with equal probability, and propose models centered around the expected OLS estimate for $\hat{\beta}^z$:*

$$\frac{\beta_R^* + \beta_L^*}{2} = \beta_{OLS} = \frac{(\beta_0 z_0^2 + \sum_{t=-T}^{-1} z_t y_t)}{\sum_{t=-T}^0 z_t^2}. \quad (4)$$

3. *Ideological polarization between the parties is given by:*

$$\beta_R^* - \beta_L^* = \frac{\sigma}{\phi(0)} \frac{|z_0|}{\sum_{t=-T}^0 z_t^2}. \quad (5)$$

We discuss each part of the proposition in turn.

No Convergence. Part 2 of the proposition is reminiscent of the classical divergence theorem from probabilistic voting models (Calvert 1985). Indeed, the proof follows an identical logic. If the parties were to propose the same model of the world, a unilateral deviation in the preferred direction would always be profitable for each of them. Depending on the realization of y_0 , this deviation will either be payoff irrelevant or strictly increase the party's expected utility. It is payoff irrelevant if y_0 is such that the deviating party loses the ideological contest, because in this case, the deviation has no impact on the ideology adopted by the voter. It improves expected utility if y_0 is such that the deviating party wins, because in this case the voter's ideology has moved in the party's preferred direction. Because parties do not know the realization of y_0 , ex ante the deviation is always strictly profitable, and ideological convergence cannot be sustained in equilibrium. Ideological polarization (here defined as the difference between β_R^* and β_L^*) always emerges.

Symmetry. Substantively, part 2 of Proposition 2 indicates that a favorable history of outcomes does not generate an advantage in the ideological contest for political parties. In our world, the two parties face symmetric strategic problems. As a consequence, the equilibrium will take a symmetric form, with the parties ex ante equally likely to win the ideological contest and persuade the voter to adopt their model of the world.

However, the results also highlight that a favorable history of outcomes does translate into an *electoral* advantage for political parties. As the history becomes more favorable to the right-wing party (i.e., the ordinary least squares [OLS] estimate for the coefficient β increases), *both* equilibrium ideologies move to the right. In turn, this improves the right-wing party's prospects of winning the election, thereby increasing its expected payoff. The converse holds if the history becomes more favorable to the left-wing party.

Finally, a corollary of the above is that some ideological manipulation always occurs in equilibrium:

Corollary 1. *For any $T < \infty$, β_R^* , $\beta_L^* \neq \beta_0$ with probability 1.*

In equilibrium, the ideologies proposed by the two parties are centered around the model that maximizes the expected fit to the history of outcomes observed by the voter. This is the expected OLS estimate for the coefficient β (which we denote as β_{OLS}), where the unobserved outcome realization y_0 is replaced by the expectation $\beta_0 z_0$. Thus, although both parties' equilibrium ideologies are a function of β_0 , because the expression in (4) includes the (random) outcome realizations, the

true model of the world emerges only in the limit where $T \rightarrow \infty$. For any finite history, therefore, neither party offers the true model in equilibrium.

Comparative Statics on Polarization. Part 2 of Proposition 2 describes the determinants of ideological polarization, that is, the difference $\beta_R^* - \beta_L^*$. Substantively, this difference captures the extent to which the models of the world proposed by the parties disagree on the consequences of the policy dimension for the voter's welfare.

We show that ideological polarization is a function of the history of policies:

Corollary 2. *Equilibrium ideological polarization:*

- *decreases as past policies become more extreme (i.e., move away from 0);*
- *increases as today's policy (z_0) becomes more extreme.*

As past policies become more extreme, historical data become more informative for the voter. If policies in the past history are close to 0, proposing a more radical ideology (i.e., a model of the world farther away from the expected best fitting one) has a small impact on the expected model fit, because the predicted outcomes under any model will be close to 0 as well. In contrast, for more extreme past policies, moving the proposed model of the world away from β_{OLS} reduces the fit to the observed history of outcomes more and, thus, also reduces the likelihood of winning the ideological contest. Radical ideologies become more costly, and ideological polarization decreases.

Consider instead the impact of today's policy extremism. Recall that parties face uncertainty over the exact realization of the outcome of today's policy, which is privately observed by the voter. As z_0 becomes more extreme, favorable realizations of the outcome y_0 have a larger (positive) impact on overall model fit. Thus, as today's policy moves away from 0, the parties can gamble on extreme outcomes and can afford to propose more radical ideologies. Ideological polarization, therefore, increases.

Finally, ideological polarization increases with the uncertainty in the true data-generating process.

Corollary 3. *Equilibrium ideological polarization increases in the variance of the distribution of the error (ϵ), σ^2 .*

As the variance σ^2 increases, the realization of y_0 becomes more uncertain from the parties' perspective. Thus, the outcome of the ideological contest becomes more arbitrary, and parties are willing to propose

ideologies that are farther away from the expected best fitting model.

An Illustrative Example: The Reconstruction Era. A key idea in our model is that political entrepreneurs strategically exploit voters' experiences and shared histories to shape the ideology voters adopt and this, in turn, shapes their policy preferences. An important example of this dynamic process comes from the Reconstruction Era in the United States. Following the U.S. civil war, formerly enslaved black freedmen gained political rights and wielded substantial political power in the legislatures of Southern states for the first time. This change in policy coincided with a sharp rise in corruption by government officials.

Although the simultaneity of these two events was coincidental and the Industrial Revolution Era rise in corruption is seen by modern scholars (e.g., Skowronek 1982) as the result of other factors,¹⁰ it was exploited by white Southern politicians to argue that black empowerment had been the cause of the increase in corruption and insider dealing. This belief became deeply embedded in the minds of many voters due to the deliberate efforts of Southern Democrats.¹¹ According to DuBois (2007, p. 511), "The Negro vote and graft were indissolubly linked in the public mind by incessant propaganda" launched by Democratic Redeemers. With this understanding of the world—this ideology—adopted by many Southerners, policy change easily followed, and black political rights were reversed soon after (DuBois 2007).

This association between black empowerment and political corruption, which was literally written into the history books by Southern historians, provided the intellectual foundation for Jim Crow and one-party rule in the South for nearly a century thereafter. The Reconstruction Era left a profound mark on American, and particularly Southern, politics, and research has established how it continues to affect modern politics (Acharya, Blackwell, and Sen 2018). It is natural to think it still runs through political ideologies today, demonstrating the importance of the ideological formation stage and the path dependence of policy that follows from this choice.

Ideology, Policies, and Dynamic Incentives. The key intuition that our article builds on is that political parties

strategically manipulate voters' ideologies in order to obtain an advantage in the electoral arena. In the baseline model, we consider a world where parties have no commitment ability. Therefore, their policy positions are exogenous and the voter's ideology influences the probability of one or the other party winning the election. However, another reason why political entrepreneurs may want to induce voters to adopt a favorable ideology is to change parties' policy stances. If the voter's ideal policy is a function of her ideology, and parties have commitment ability, moving the voter's ideology will shift the platforms that parties propose in equilibrium.

In the SI E.2 (p. 15), we analyze this version of the model. Here, the parties no longer face a symmetric problem in the ideological contest. Proposing a more extreme ideology decreases the probability the party can persuade the voter but, conditional on doing so, moves the voter's optimal policy *and* the equilibrium of the platform game in the party's preferred direction. The net gain (or cost) is a function of how far the party's own ideal point is from the voter's induced preferences. Although this complicates the analysis, we nonetheless show that the nature of the parties' strategic incentives is analogous to those emerging in the baseline model. Thus, ideological polarization always emerges in equilibrium, and increases as the history of policies becomes more informative (i.e., extreme).

Further, we analyze a dynamic version of the game where the history of past policies is (partially) endogenized, to study how the prospect of engaging in an ideological battle influences parties' incentives to propose moderate or extreme platforms. We show that, in equilibrium, the party that is favored by the true model of the world proposes more extreme policies to facilitate voter learning, even at the cost of decreasing the chances of winning the upcoming election. The party sacrifices immediate electoral success in order to move the equilibrium of the ideological contest in his preferred direction, and thus obtain better policies in the future, similarly to Izzo (2022).

The Multidimensional Model

So far, we have assumed that parties are constrained to include only the policy dimension z in their models of the world. Real-world ideologies often weave in nonpolicy dimensions of the social world. We aim to capture this richness here, and to understand what happens to equilibrium polarization as models of the world become more complex and expand to encompass more features of the environment.

¹⁰An unfavorable realization of ϵ , in the terms of our model.

¹¹In this interpretation, in the true model is no relationship between this policy dimension (black political rights) and the outcome (corruption). The observed history indicated a positive relationship and this allowed Southern politicians to offer such an ideology and have it accepted by voters.

In this section, we allow parties to include in their models, in addition to the policy variable z , an additional vector-valued set of covariates \mathbf{x} . The key distinction between policy and covariates is that the policy dimension z is the one over which parties have preferences and/or are differentiated, and on which they have control. Nonpolicy covariates may nonetheless be relevant because of the possibility that they affect outcomes. For example, we may think of some components of \mathbf{x} as immutable ethnic, cultural, or demographic characteristics of the population. Alternatively, covariates may represent exogenous features of the environment, such as the state of the global economy, or geopolitical factors. These elements cannot be altered by policy means (at least in the short run), but parties may nonetheless find it useful to include them in equilibrium ideologies if they help to explain variation in outcomes.

In this section, we ask if and when parties choose to include nonpolicy variables in their models, and whether conflict on these dimensions emerges in equilibrium, that is, whether the proposed models differ on nonpolicy dimensions. Furthermore, we analyze whether there is an association between model complexity and ideological polarization in equilibrium.

The generalization from the one-dimensional setting is that the data-generating process is now taken to be $y_t = \beta'_0 w_t + \varepsilon_t$, where

$$w_t \equiv \begin{bmatrix} z_t \\ \mathbf{x}_t \end{bmatrix},$$

and \mathbf{x}_t is a k -dimensional vector of attributes. Without loss, we assume that the mean of each dimension of \mathbf{x} is zero. It will be useful in what follows to define the stacked $(T \times (k + 1))$ matrix of history W , where each row of W is an observation of w_t for $t \in \{-T, \dots, -1\}$, and similarly the “extended” history W_+ equal to W with an additional row $w_0 = (z_0, \mathbf{x}_0)$.

Each party i proposes a vector of coefficients β_i of dimension $k + 1$. We use the superscript j to denote the j -component of β_i . Thus, β_R^z is the z -coefficient proposed by the R party. Note that the model need not encompass all available dimensions, as proposing a coefficient $\beta_i^j = 0$ is equivalent to excluding dimension j from the model of the world. As in the baseline setup, the voter selects the ideology that best explains, in the likelihood sense, the history of outcomes she observes. Importantly, we do not assume that the true coefficients $\beta_0^j \neq 0$, that is, we allow for the possibility that some dimensions of \mathbf{x} 's true correlation with outcomes y are 0. Initially we will take the set of covariates included in the common-knowledge history to be exogenous; Later we will endogenize the choice of what to make available.

Analysis

Proposition 3 establishes the multidimensional equivalents of each part of Proposition 2. As a result, the main comparative static results from the baseline single-dimensional setup (Corollaries 1–3) will continue to hold in the multidimensional setting.¹²

Proposition 3. *If W has full rank and $w_0 \neq 0$, then a Nash equilibrium exists. In any such equilibrium:*

1. *the two parties' models of the world differ on all dimensions. $\beta_R^{j*} \neq \beta_L^{j*} \forall j$;*
2. *the parties always win the ideological contest with equal probability, and propose models whose z -component centers around the expected OLS estimate for β^z :*

$$\frac{\beta_R^z + \beta_L^z}{2} = ((W'_+ W_+)^{-1} W'_+ y_+)^z,$$

$$y_+ \equiv \begin{bmatrix} y \\ w'_0 \beta_0 \end{bmatrix};$$

3. *ideological polarization on all dimensions between the parties is given (implicitly) by the solution to the vector equation:*

$$\beta_R - \beta_L = \frac{\sigma}{\phi(0)} \frac{|w'_0(\beta_R - \beta_L)|}{\beta_R^z - \beta_L^z} (W'_+ W_+)^{-1} \begin{bmatrix} 1 \\ 0 \\ \vdots \\ 0 \end{bmatrix} \quad (6)$$

In addition to preserving the results established in one dimension, the multidimensional environment delivers some new comparative static results on which we now expand.

Complete Politicization. Part 3 of Proposition 3 shows that equilibrium ideologies are always total: All available nonpolicy dimensions are always included (in the sense of having nonzero coefficient in β_i) by at least one of the parties, and the models offered by the parties differ on all dimensions. Because the size of the history is finite, the within-sample correlation between each x^j and z is always nonzero.¹³ Therefore, the (expected) OLS estimate for β^z is a function of whether x^j is included in the model, and because equilibrium proposals move with the expected OLS, at least one party will have an incentive to include it.

¹²Corollaries 1–3 hold locally, close to the mean value of the \mathbf{x} 's. The implicit expression in (6) reduces to an explicit one in one dimension, such that the corollaries can be stated unconditionally. In the general case, we rely on the implicit function theorem to establish local comparative statics close to the mean of the data.

¹³Outside of a set of outcomes with probability zero.

The intuition for divergence is that parties can use the x dimensions to improve the overall fit of their model, and take advantage of this better fit to push for more extremism on the policy dimension. In other words, parties increase the dimensionality of their model so as to blame policy failures on unrelated factors. Consider the incentives facing the right-wing party. The party trades off the desire to induce the voter to adopt an extreme right-wing ideology on the z dimension, with the need to win the ideological contest. Suppose that x^j and z are positively correlated, with an analogous argument holding for the mirroring case. Then, the cost of ideological extremism on the z dimension can be partially offset by proposing a low coefficient on x^j .¹⁴ Given the positive correlation with z , this tends to move predicted outcomes closer to the observed history, thereby improving the overall fit of the model. Directionally opposite incentives emerge for the left-wing party. As a consequence, the parties' models of the world always differ on the x^j dimension. Specifically, the sign of the element of the covariance matrix corresponding to the pair (z, x^j) determines the role that x^j plays in the parties' narratives:

Corollary 4. *Suppose the element of the within-sample inverse covariance matrix $(W_+^* W_+)^{-1}$ corresponding to the pair (z, x^j) is positive. Then, in an open neighborhood around the line $w_0 = [z_0, 0, 0, \dots, 0]$, $\beta_R^j > \beta_L^j$. The converse also holds.*

In the simple bivariate setting (with scalar x), the (z, x^j) element of the inverse covariance matrix has the opposite sign as the correlation between the two variables. So, an x that is positively correlated with z will be emphasized more by the left-wing party than the right ($\beta_R^j < \beta_L^j$) and vice versa.

Additionally, although all available dimensions are politicized in equilibrium, some are more politicized than others. The larger is the correlation between policy and covariate in the history, the larger will be the parties' polarization on that dimension. This statement is Corollary 5.

Corollary 5. *The stronger the (within-sample) correlation between x^j and z , the larger is the magnitude of the difference in equilibrium coefficients on the j dimension, $|\beta_R^j - \beta_L^j|$.*

Model Complexity and Ideological Polarization. Following the logic above, parties use additional dimensions to compensate for more extremism on the policy dimension. A consequence is that adding additional dimensions

to the history allows the possibility of greater observed polarization on the policy dimension. It turns out that in equilibrium, there is an association between model complexity and ideological polarization, which is conditional on the realization of the last-period policy and covariates:

Corollary 6. *Let $\tilde{W}_+ \equiv [W_+ x^{k+1}]$, and let $w_0 = [z_0, 0, 0, \dots, x_0^{k+1}]$. The ratio of equilibrium ideological polarization on the z dimension under \tilde{W}_+ to that under W_+ is:*

$$\frac{\tilde{\beta}_R^z - \tilde{\beta}_L^z}{\beta_R^z - \beta_L^z} = \begin{cases} r \geq 1, & x_0^{k+1} = 0 \\ r > 1, & \text{sign}(z_0) = \text{sign}(x_0^{k+1} (W_+^* W_+)^{-1}_{z, k+1}) \\ r > 0, & \text{sign}(z_0) \neq \text{sign}(x_0^{k+1} (W_+^* W_+)^{-1}_{z, k+1}). \end{cases}$$

Substantively, Corollary 6 says that when today's realization of policy and covariates aligns with the pattern observed in the historical data, observed polarization is higher than it would be without the additional covariate. When there is a "surprise," in the sense that the correlation today is in the opposite direction of the historical pattern, polarization may be lower. If the realization of the covariate today is exactly at its mean (0), there is a weakly positive effect on polarization of adding the additional covariate.¹⁵ If the period 0 realization is drawn from the same conditional distribution that generated the history, a surprise is unlikely, and thus the additional covariate on average increases polarization. We thus expect the addition of more complexity in parties' models to generally increase observed polarization.

Endogenous Salience. In the model analyzed in the previous section, it is costless for parties to propose more complex models. Consequently, even when the correlation with the policy dimension z is arbitrarily small, parties will always choose to include all available variables in their narratives, and ideologies are always total.

Here, we instead consider that parties must pay a cost to render nonpolicy dimensions salient in the voters' views, and that additional dimensions can play a role in ideologies only when they are salient.

We thus add an additional stage to the game, occurring prior to the ideological contest. In this stage, either party may pay a cost C to make nonpolicy dimension x available in the history. If at least one party pays the cost, then the parties play the multidimensional version of the game; otherwise they play the baseline unidimensional game. We interpret C as the cost of informing the voter of the past history of x , through a campaign of public education (or propaganda, depending on one's point of

¹⁴That is, low relative to the OLS estimate on this dimension.

¹⁵The effect is strictly positive except in the case that x^{k+1} is orthogonal to z in the observed history.

view).¹⁶ Absent such costly efforts, the voter is unaware of the history of x , and will not be able to use the x dimension when computing the predicted outcomes under the parties' models of the world. Therefore, parties cannot gain from including this additional dimension in their ideologies unless and until the voter is made aware of its past history.

We show that, in equilibrium, x will become politically salient if and only if the within-sample correlation with z (and y) is sufficiently large. Denote β_{OLS}^z the (expected) OLS estimate for β^z if x is included in the model, and $\beta_{Omitted}^z$ the estimate from the single-dimensional model. The difference $\beta_{Omitted}^z - \beta_{OLS}^z$ is the omitted variable bias, which we denote as Δ .

Proposition 4. *There exists a unique threshold $|\widehat{\Delta}|$ such that the nonpolicy dimension x becomes endogenously salient if and only if $|\Delta| \geq |\widehat{\Delta}|$.*

As discussed in relation to Corollary 4, parties include nonpolicy variables in their models in order to exploit the within-sample correlations and move the equilibrium ideology in their preferred direction. Suppose $\beta_{Omitted}^z - \beta_{OLS}^z < 0$, so that the omitted variable bias moves the estimate to the left. Then, the right-wing party benefits from making x politically salient. However, for the party to be willing to pay the cost C , the magnitude of the bias (and thus the correlation between variables) must be sufficiently large. An analogous reason applies to the left-wing party when $\beta_{Omitted}^z - \beta_{OLS}^z > 0$.

The results of this section highlight that random events may have a crucial importance in the genesis of political ideologies. Recall that parties have no control, or preferences, over the nonpolicy dimension. Therefore, if a strong enough historical correlation with the policy variable (and thus a large enough omitted variable bias) emerges, it is purely by chance. Political parties, acting as ideological entrepreneurs, will exploit such correlations between variables to their favor, constructing complex models of the world that support their favored policy position. Furthermore, Proposition 4 indicates that the sign of the historical correlation with the policy dimension will determine how the parties position themselves on other issues. Thus, random historical events will determine how social issues, religion, race, and other issues become integrated into political ideologies.

An Illustrative Example: The Politics of Nostalgia. The multidimensional model shows that the ideological debate is in part a contest over which dimensions voters

¹⁶Qualitatively equivalent results would obtain if, prior to the ideological contest, each party decides whether to invest a cost in order to increase the dimensionality of its own model.

should pay attention to. An example from modern American politics illustrates this feature in practice.

Pat Buchanan, the Republican political operative and avatar of the "paleoconservative" wing of the party, wrote in *Suicide of a Superpower* (2012, p. 44):

How, in a generation, did we reach a point where. . . our children will not know the good life their parents had, [where] the American Dream may never become reality for scores of millions of our countrymen?

The answer: the failure of our system is rooted in a societal failure. We are not ruled by the same ideas nor do we possess the same moral character as our parents did . . . our intellectual and cultural elites reject the God our parents believed in and the moral code they lived by.

Buchanan's book, like much American social-conservative rhetoric, explains the country's supposed decline from the prosperous and optimistic years of the 1950s as the result of the country's deviation from traditional family and moral strictures. In Buchanan's telling, the American golden age is in the past, lost due to the increasing degeneracy of a godless cultural elite and its corrupting influence on the public's moral character. Importantly, in this understanding the lamented decline is not to be attributed to economic policy changes since the 1950s, such as reductions in the top marginal income tax rates, budget cuts to public institutions, or the relaxation of antitrust enforcement.

In the logic of our model, two features of this rhetoric stand out. The first notable feature is that Buchanan's statement contains no reference to any particular policy. It instead invites the audience to adopt a model of the causal forces that underlie the variation in outcomes they observe in the world. This is consistent with how we represent the ideological contest in our model. The second notable feature is that, in presenting an ideology, Buchanan is arguing for a particular weighting of dimensions in how voters see the world that allows him to attribute blame away from conservative economic policies. This aligns with the logic underlying our multidimensional narratives.

Conclusion and Discussion

In this article, we have developed a model of hierarchical policy preference formation, where parties provide causal explanations (ideologies) for patterns observed in voters' past experience. Voters evaluate these ideologies according to their fit to experience, and then use the best fitting

one when deciding which policies to support. Winning the ideological battle thus confers an advantage in subsequent electoral competition. The advantage of political parties over voters in our model is a technological rather than an informational one: Their exclusive control over the creation and dissemination of ideologies grants parties some ability to persuade even in the absence of any private information.

This persuasive ability is constrained by the features of the common-knowledge history of outcomes. A lower degree of policy extremism in the history means the data are less informative about the effects of policy, which in turn allows parties to offer more divergent ideologies. The persuasive ability of elites is also determined by the history that is considered politically relevant. We showed how ideology can be shaped by variables that are beyond the control of politicians, and even issues that are not inherently political, as long as they are correlated and, to an uninformed voter's mind, plausibly related.

In concluding this article, we briefly discuss how our model may be enriched and how our conceptualization of ideology further exploited to improve our understanding of the formation of policy preferences, polarization, and electoral competition.

History, Ideology, and Policy Preferences

One valuable contribution of the model is to help understand why the construction of consensus history and its dissemination in schools and universities is so often hotly politicized. Even in a world of perfect information about parties' policy agendas and no commitment to platforms—where what parties will do if given power is perfectly predictable *ex ante*—what citizens know about the past can change how they respond to party rhetoric, and ultimately which party they are willing to support. Strategic politicians and political movements understand this dependence well, and intervene when they can to shape the “dataset” that future voters draw upon.

Intriguingly, this suggests that the relationship between voter knowledge and political outcomes is conditional on the type of information held. On one hand, a longer memory of policy history reduces polarization as voters draw upon a larger time series of data to tighten their beliefs about the underlying world. On the other hand, a broader knowledge of other variables, whether policy related or not, may increase polarization as parties are better able to fit the policy variable to their preferred ideology. Proposals to improve policy making by expanding voter knowledge depend critically, therefore, on the direction of knowledge expansion.

Ideological Persuasion, Ideological Revision

To streamline the presentation and focus on the key logic underlying parties' ideological competition, we have focused on a one-period game. Altering the model so that the game is repeated more than once, with a fresh ideological contest in every period, does not impact the results. As in the one-shot model, parties have symmetric yet directionally opposed incentives to pull the voter to the extreme. This then drives results qualitatively identical to those presented above (see Appendix E.4.1, SI p. 25).

A perhaps more meaningful way to think about dynamics in our setting is to consider a world where, once it is formed, ideology is sticky, but can be called into question if it does not resonate with the voter's future experiences. Here, when engaging in the ideological contest, parties think about persuading the voter today *and* ensuring their proposed model of the world is not susceptible to being revised in the future. This may alter their incentives in two ways. First, both parties may be pushed toward the true model. Second, parties may have asymmetric incentives to avoid ideological revision, depending on whether they believe the outcome of a new ideological contest would be more or less favorable to them than the current situation. In turn, this possibility would influence parties' preferences over policies, creating an additional set of dynamic incentives. Analyzing this richer setting is certain to prove technically challenging, but is particularly promising for future research. In the SI (E.4.2, p. 27) we take a first step in this direction. We show that, as expected, the parties no longer face a symmetric problem in the original ideological contest. The party that is disfavored by the history in the first period would like to encourage ideological reassessment in the future, and it moves its ideology toward the truth, albeit at the cost of some reduction in the probability of winning the first-period contest. Despite this asymmetry, we are able to show that, under some conditions, the comparative statics from the baseline model continue to hold.

Groups and Identity

We have operationalized ideology as a theory of how the world works, albeit with potentially rich understandings that incorporate many variables and that may extend beyond politics. It is possible that one's ideology is chosen in conjunction with one's identity and even membership of a group (Mason 2018). If identity and group membership are chosen first, then this will shape the beliefs voters bring to politics and how they experience

and perceive the history that, in turn, affects how they respond to ideologies proposed by the parties.¹⁷

One simple extension of our model is to suppose that society consists of two different identities—say, conservative and liberal—that manifest as two distinct groups. The true data-generating model is different for the different groups, for example, the same policy may in expectation help one group but hurt the other. Thus, all members of the same group share a common history, which is distinct from the one observed by the other group. The parties must now weigh how the different groups will evaluate the ideology a party offers and in which group will the median voter reside at the election.¹⁸ We conjecture that the existence of heterogeneous groups in society has the effect of increasing ideological polarization in equilibrium. The uncertainty about how the median voter will interpret ideologies adds to the other uncertainty in the model, and this empowers the parties to diverge further in their ideological offerings. The increase in polarization is larger the more evenly divided are the groups.

In the equilibrium of this expanded model, the two groups will, with high likelihood, adopt different ideologies, with each adopting the ideology of a different party. That the divide between the groups extends beyond policy preferences to their underlying views of the world resonates with the current state of American politics. This extension of the model may go some way to explaining the hollowing of the middle in the U.S. electorate that emerged in recent decades and why the two sides of politics so often seem to talk past each other, unable to communicate. Formally analyzing this richer setting is thus an important avenue for future research.

Values versus Ideology

An important assumption in our model is that a citizen's objective is taken as given. Thus, she knows what outcome she wants to achieve and her uncertainty is only over the policy tool that achieves it. Ideology in our model is, therefore, a practical ideology, concerned with the pragmatics of achieving particular outcomes. It does not concern itself with the values of the citizenry, which are taken as fixed. As mentioned in the introduction, this represents the narrow view of ideology, and is a subset of

broader conceptions of ideology in which values are also at stake (Bonilla-Silva 1997).

To expand our framework to endogenize values as well, we can think of an ideological hierarchy in which different principles and beliefs are laid down sequentially. People first formulate their values from experience and some innate metric of happiness or meaning. The values so constructed can then inform or constrain the beliefs about the world that are the focus here and, in turn, shape policy preferences and political behavior. It is an open question how this hierarchy is best formalized, whether it is a purely sequential set of decisions or whether there is some overlap or feedback between levels, as Bonilla-Silva (1997) seems to suggest. Applying our formal structure to this question, and connecting to the myriad accounts of ideology in the literature, is a promising direction for future work.

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¹⁷An alternative possibility is that identity and membership of a group are chosen simultaneously with ideology.

¹⁸The model we present in the article can be interpreted as the case in which one group dominates the other and holds the median voter with certainty.

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Supporting Information

Additional supporting information may be found online in the Supporting Information section at the end of the article.

Appendix A: Proof of Proposition 1

Appendix B: Proof of Propositions 2 and 3

Appendix C: Proofs of Corollaries 1-5

Appendix D: Proof of Proposition 4

Appendix E: Extensions and Robustness